

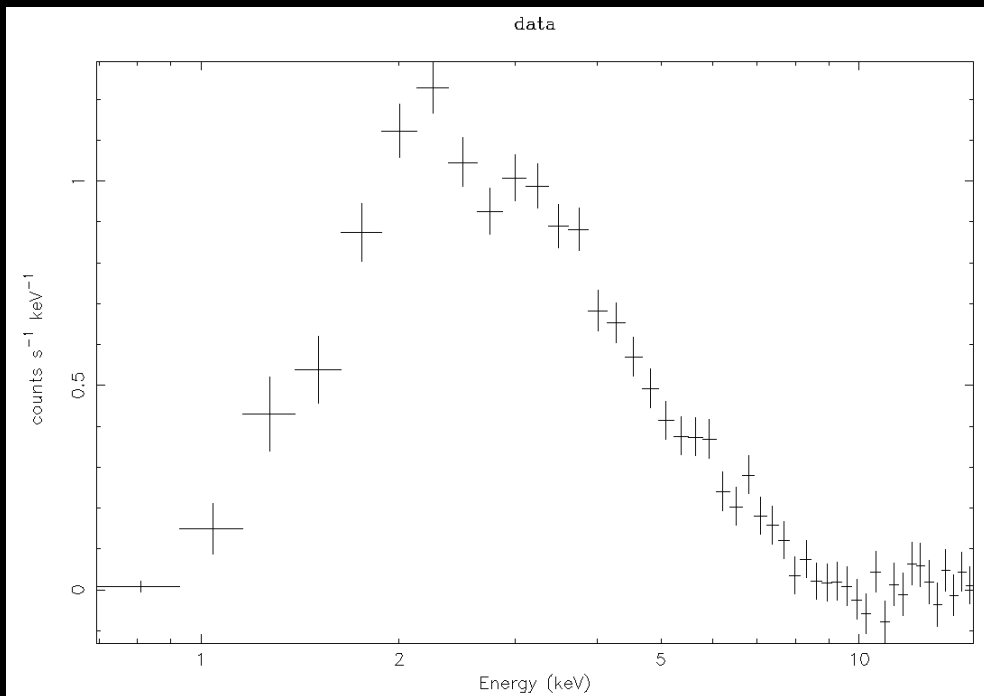
# Pitfalls and solutions to model miss-specification in X-ray spectral modelling

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Matteo Lucchini

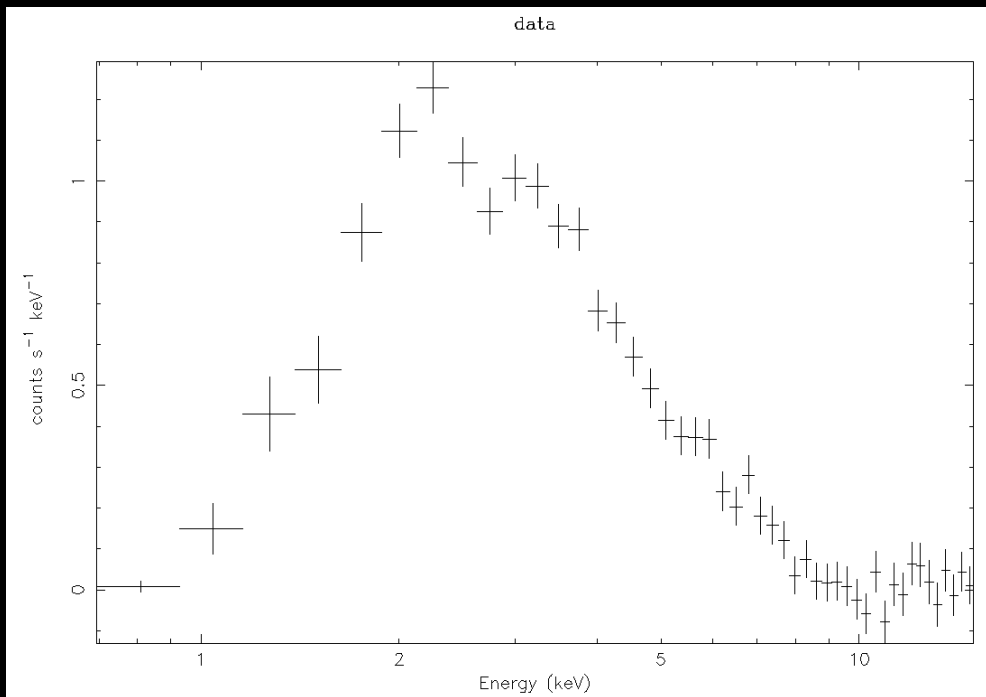
# X-ray data has changed

Legacy data: low S/N, spectra only

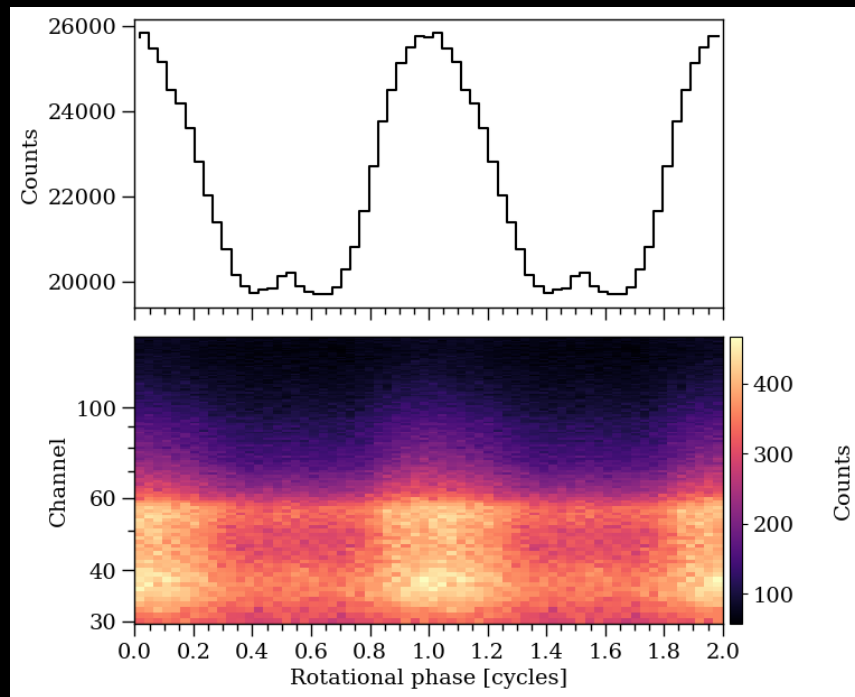


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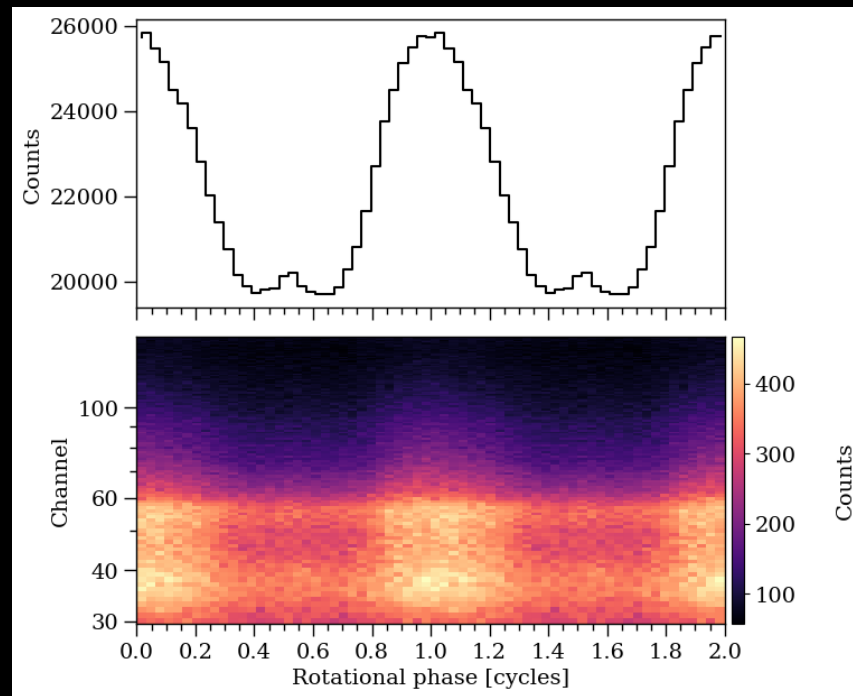
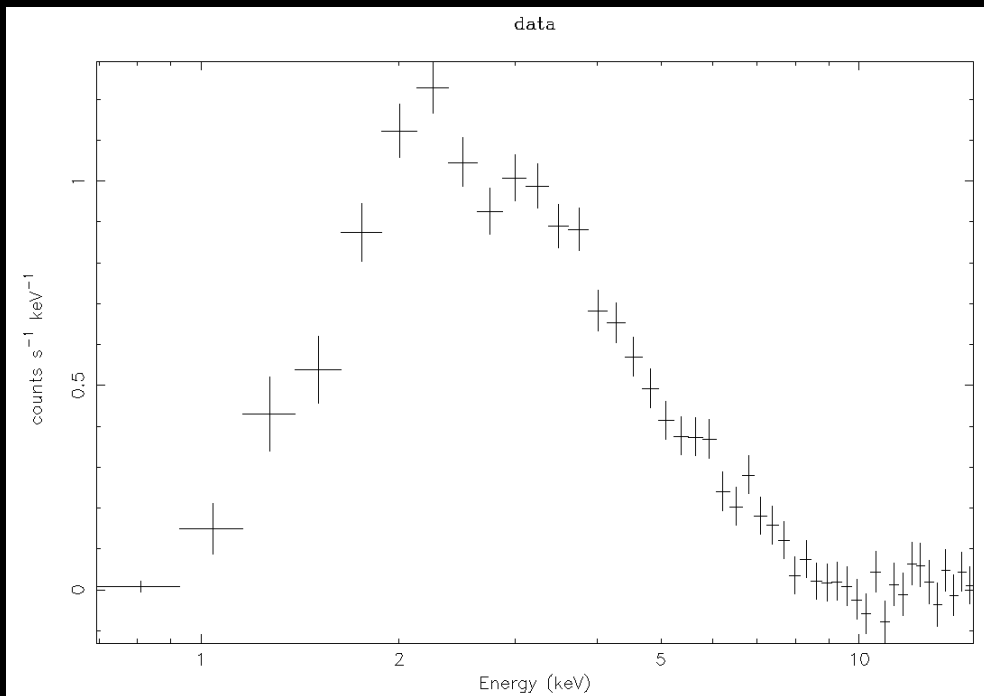


Modern data: high S/N, two+ d

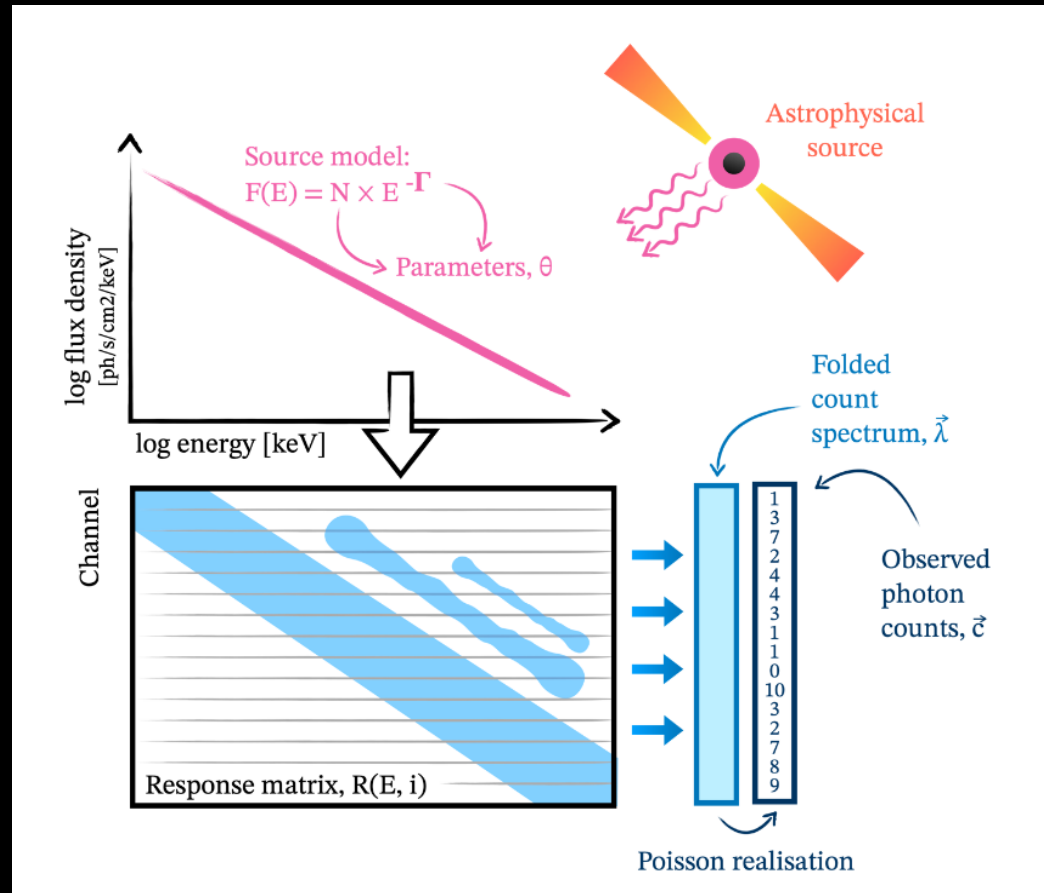


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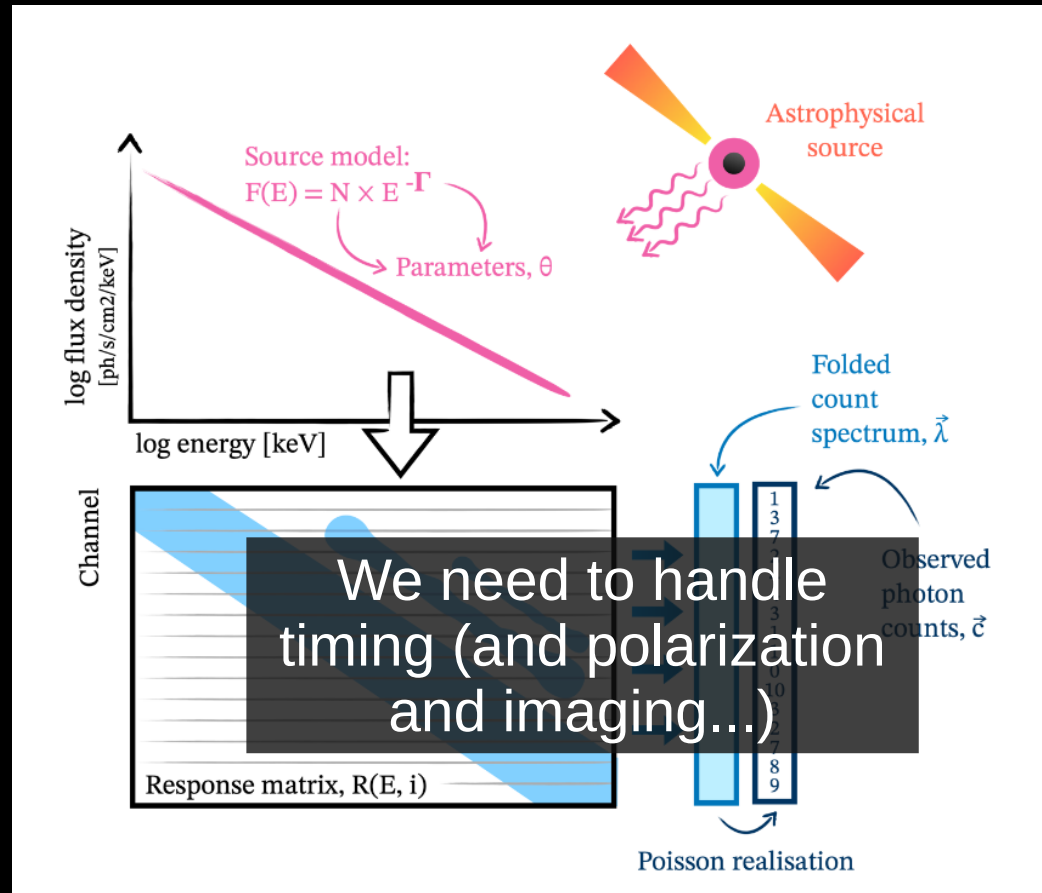
Our software has not changed, our data (and models) have



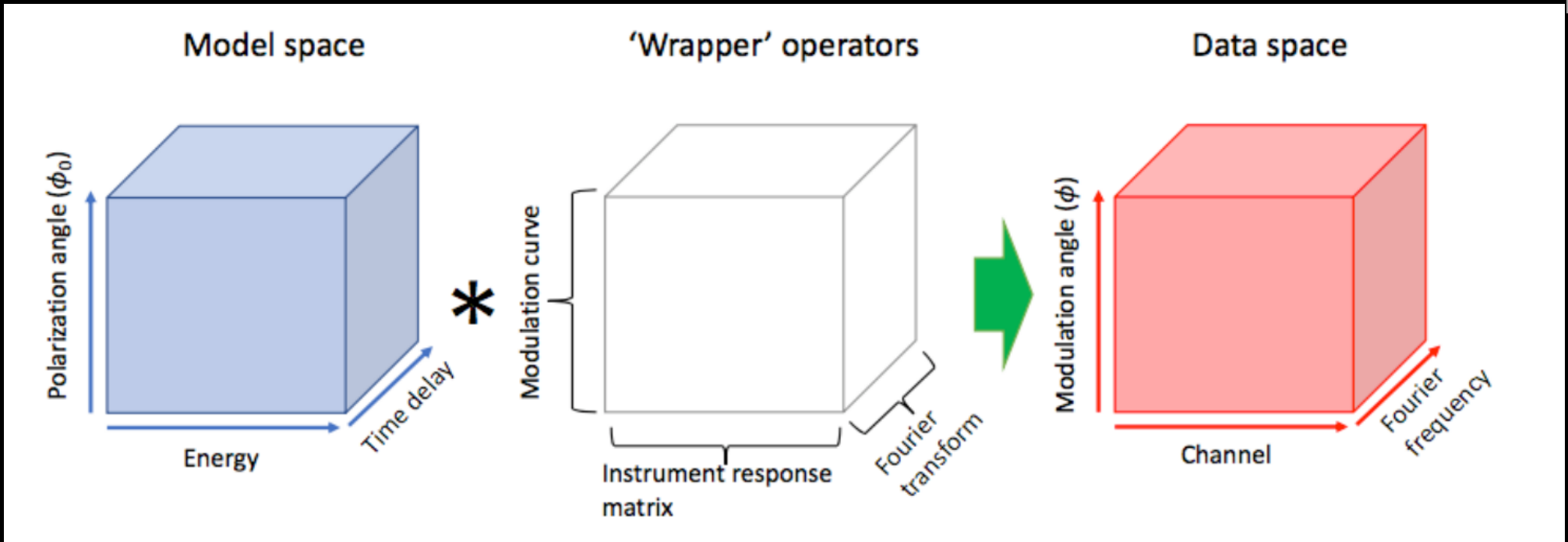
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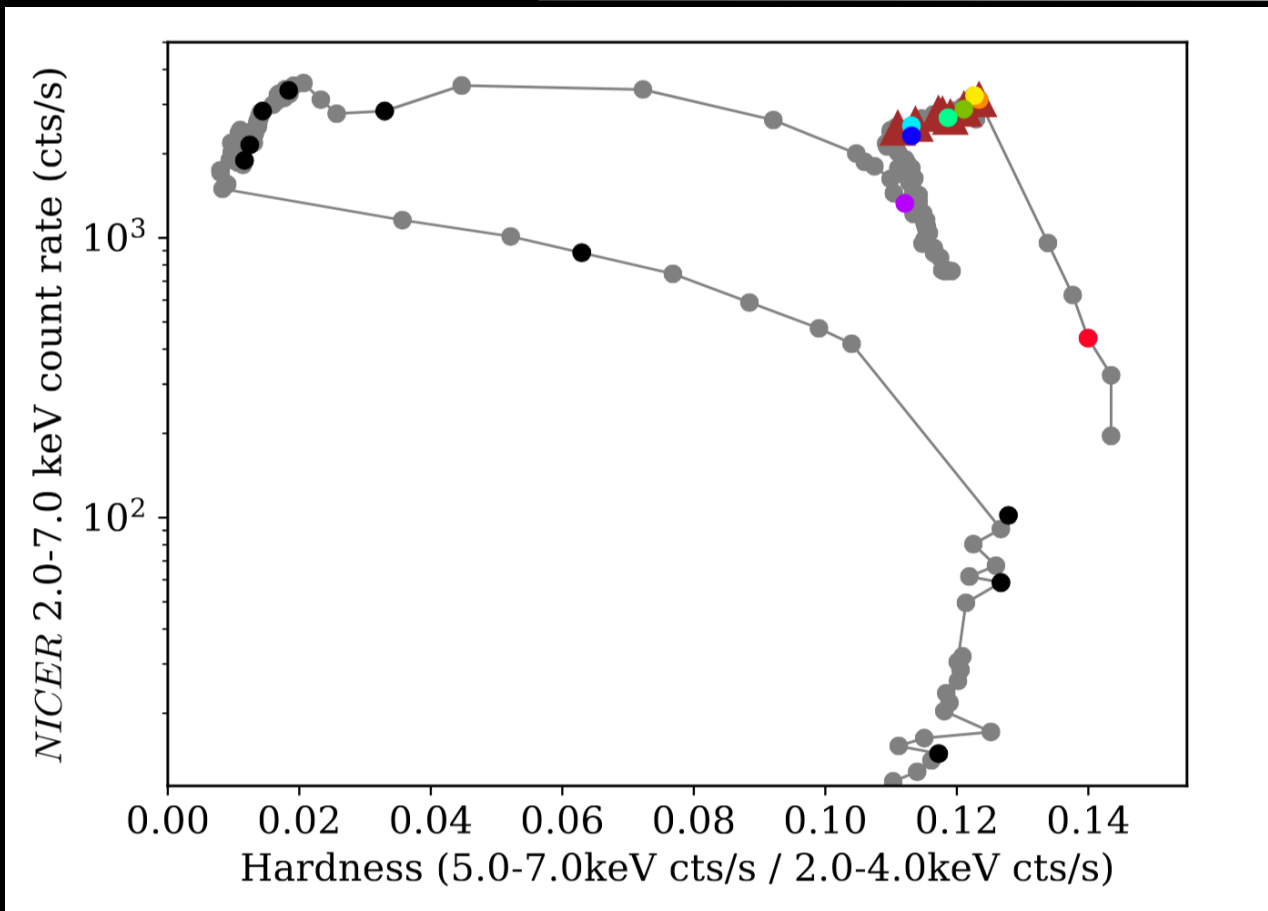


# nDspec: nD data+models

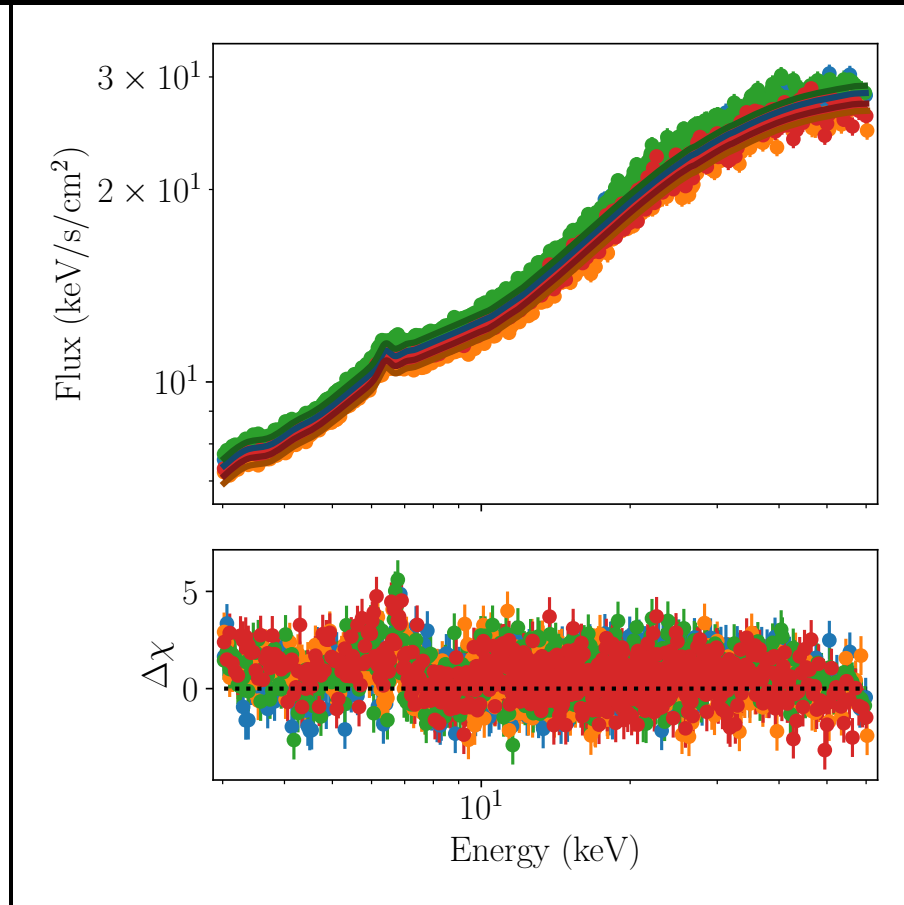
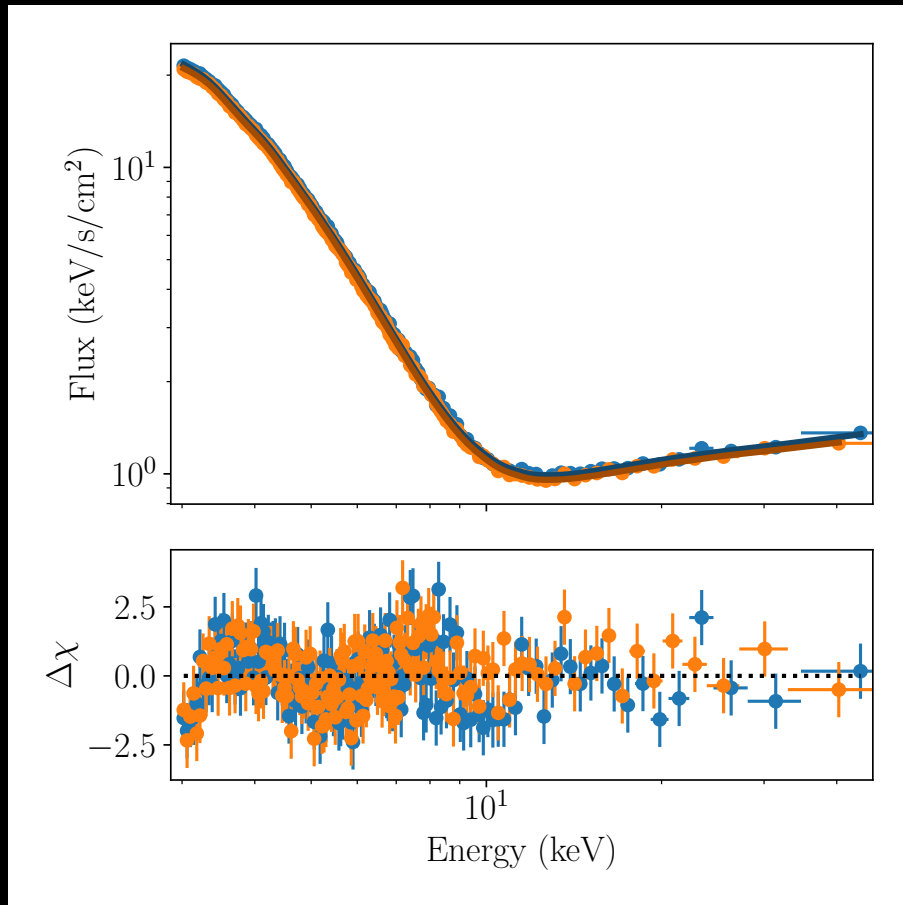


- Generalize handling instrument responses to “Operators” in all dimensions
- With data complexity we also need better sampling ability!
- 25% of the funding from NewAthena

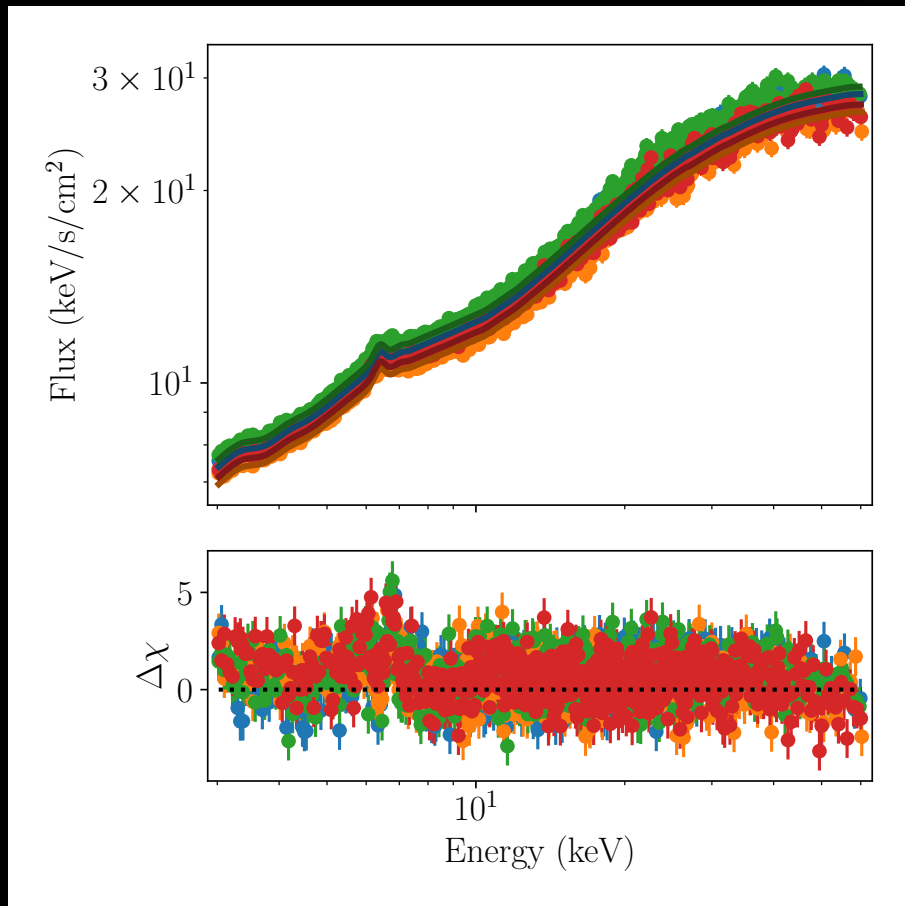
# A standard case: relativistic modelling



# Found a decent fit...now what?



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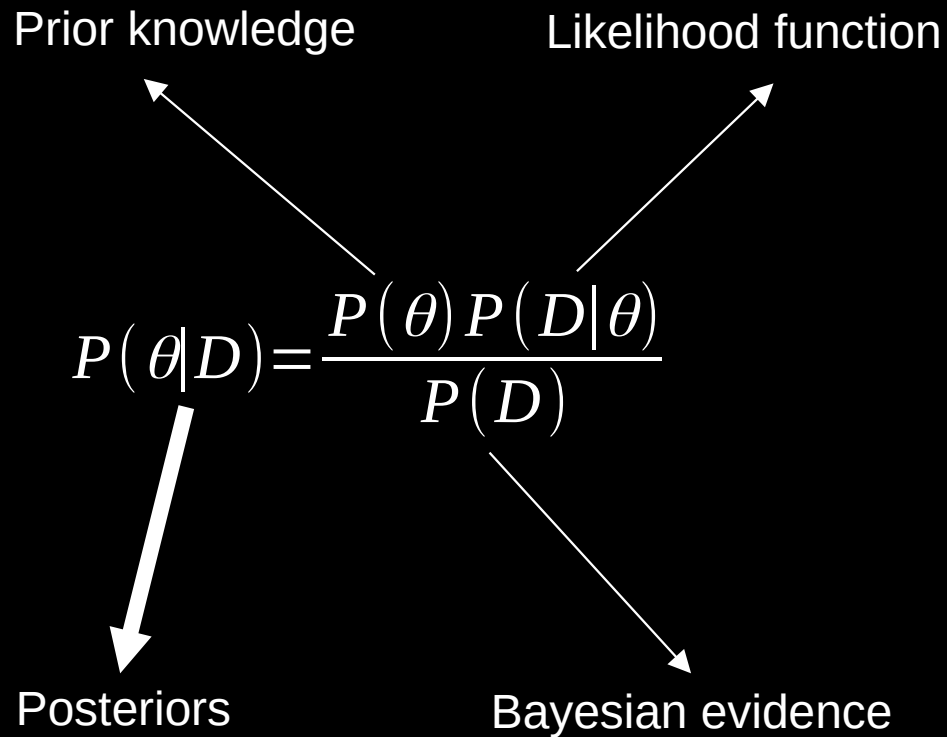


How well constrained are my parameters?  
Can I measure spin here?



Time for Bayesian sampling!

# A recap of Bayesian inference



# A recap of Bayesian inference

Prior knowledge

Likelihood function

$$P(\theta|D) = \frac{P(\theta)P(D|\theta)}{P(D)}$$

We need to find clever ways to find the “right”  $\theta$ , then calculate  $P(\theta)$  and  $P(D|\theta)$

$P(D)$  is for model comparison (and a bit difficult to calculate)

Posteriors

Bayesian evidence

# A recap of Bayesian inference

$$P(\theta_i|D) = \frac{\int_{i \neq j} P(\theta_j) P(D|\theta_j) d\theta_j}{P(D)} \quad \leftarrow \text{Marginalization}$$

Inference is just one giant Monte Carlo integration problem!

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Two main approaches in the field:

1) MCMC: draw samples in some clever way to estimate the integrals more easily

2) Nested sampling: reduce the problem to a 1D problem

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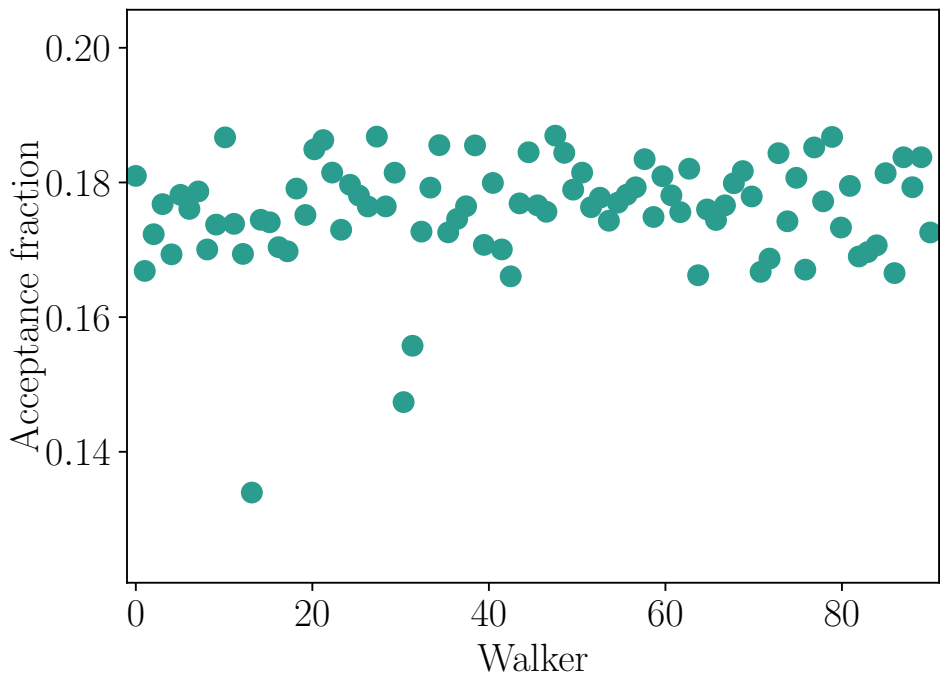
Regardless of method, convergence is key! Need to minimize Monte Carlo errors!

# Convergence issues

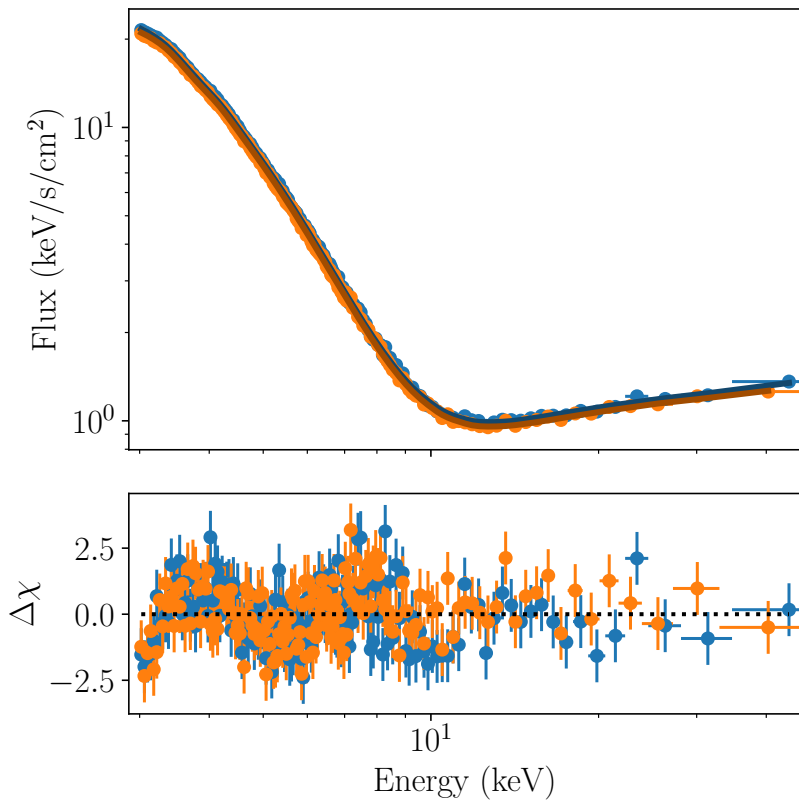
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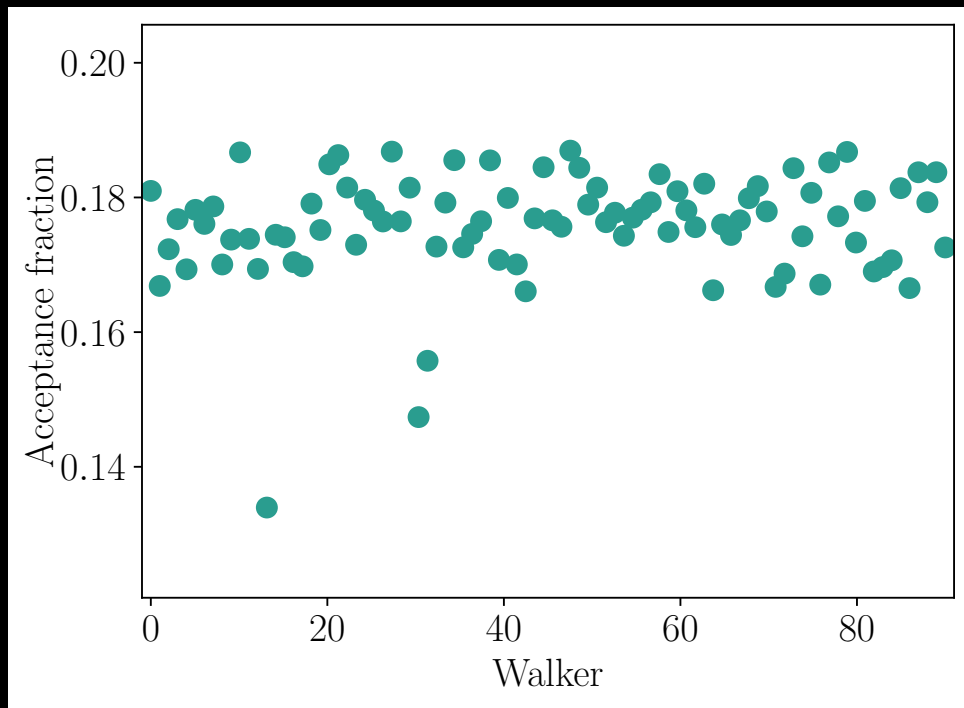
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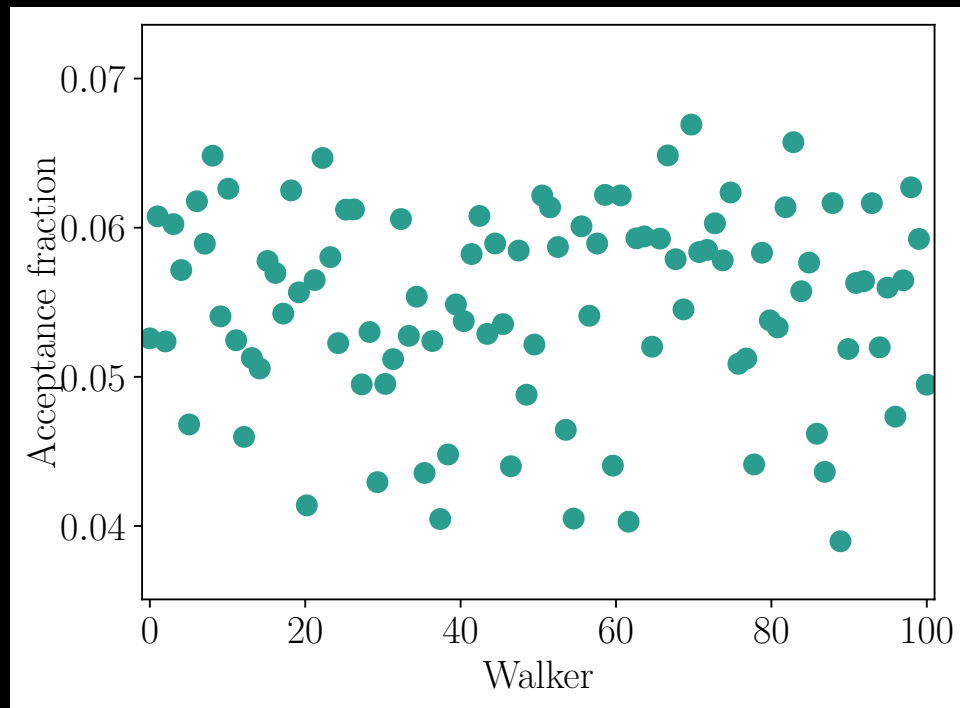
Fixed spin: reasonable behavior



# Convergence issues



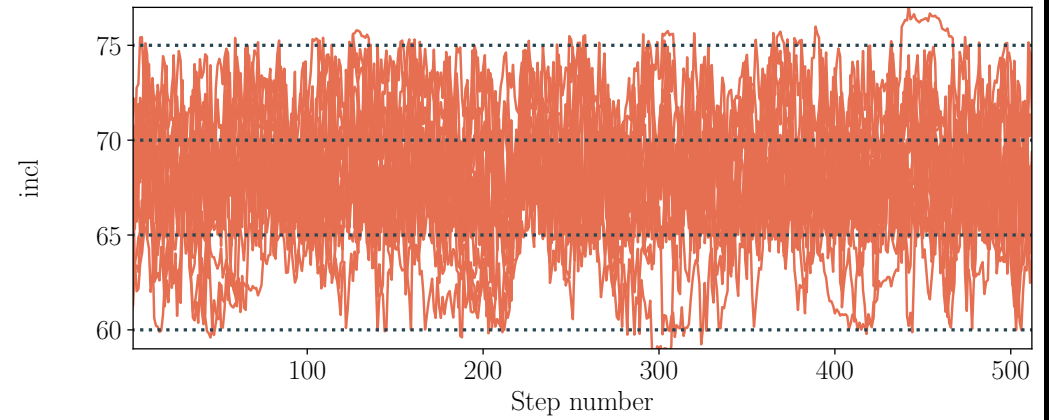
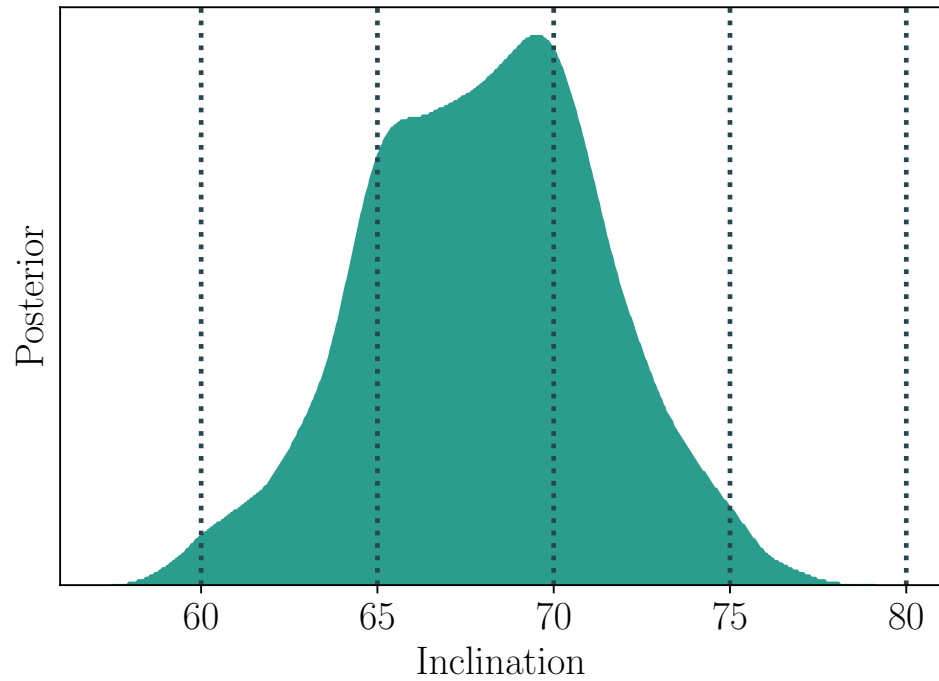
Fixed spin: reasonable behavior



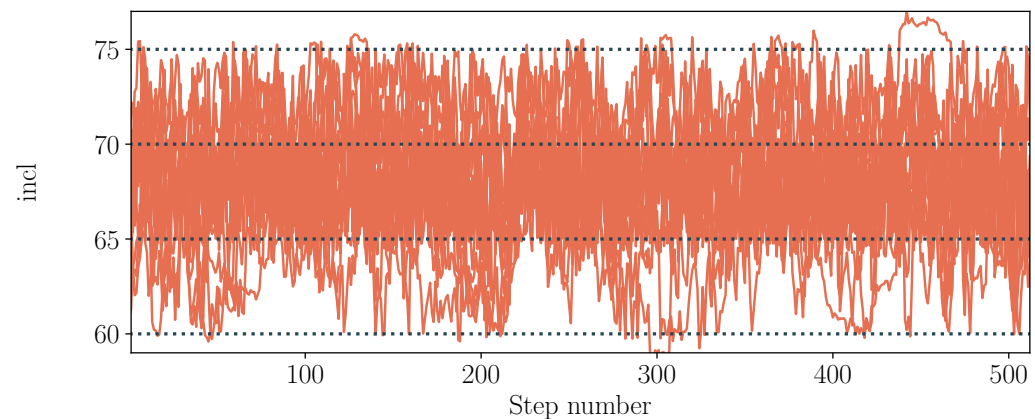
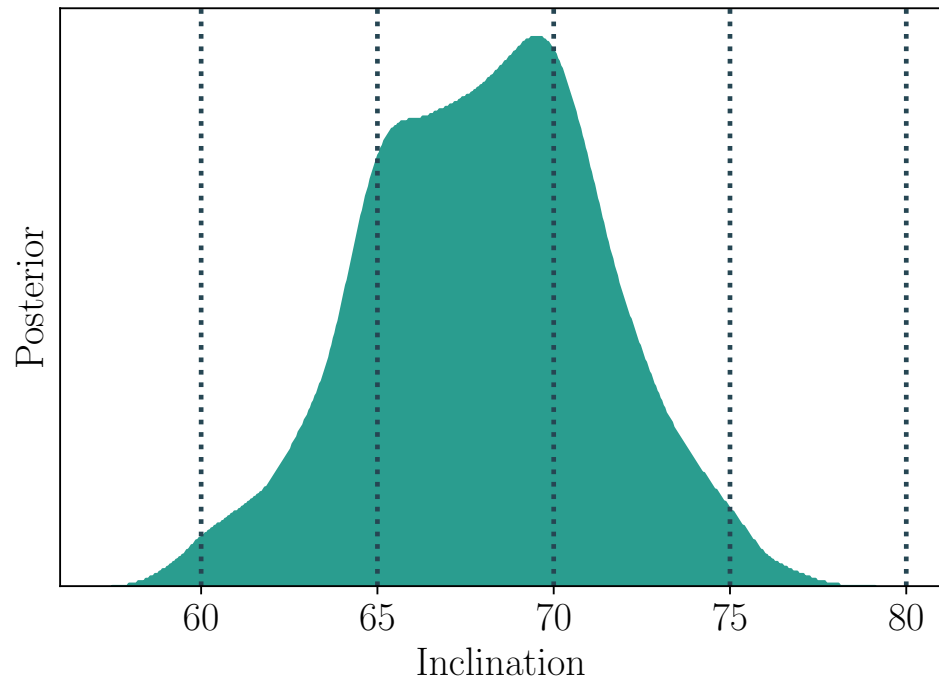
Free spin: uuuuuuh....

“If the acceptance fraction is getting very low, something is going very wrong.”

# Problematic results: kerrbb



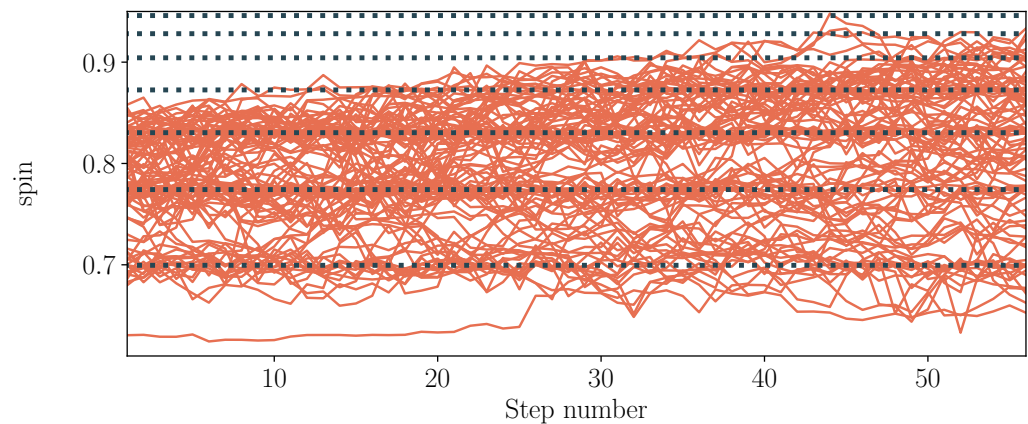
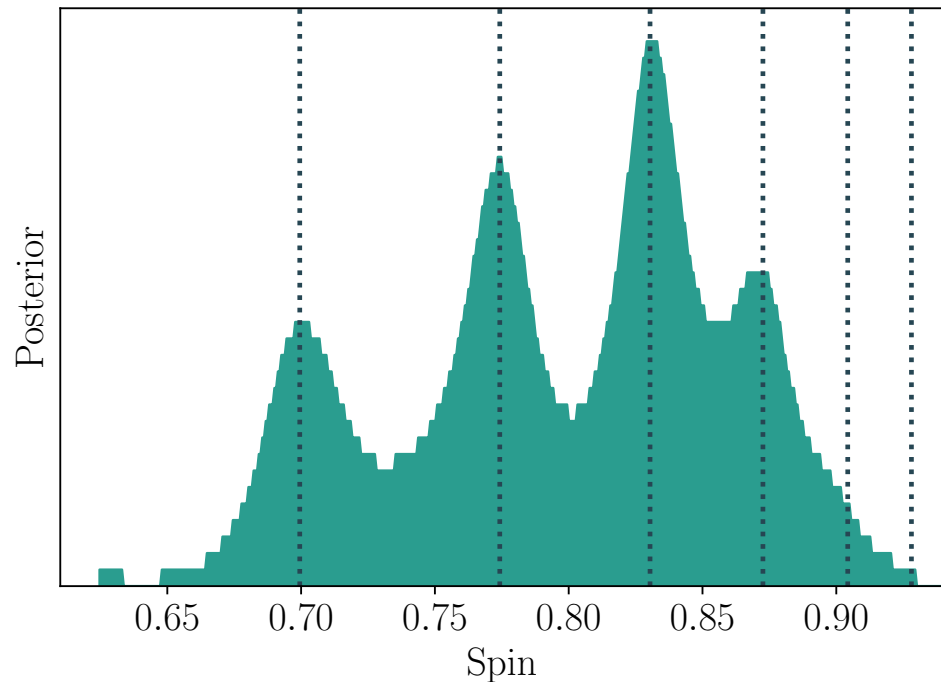
# Problematic results: kerrbb



The dotted lines are grid points in kerrbb

The walkers cluster artificially around them!

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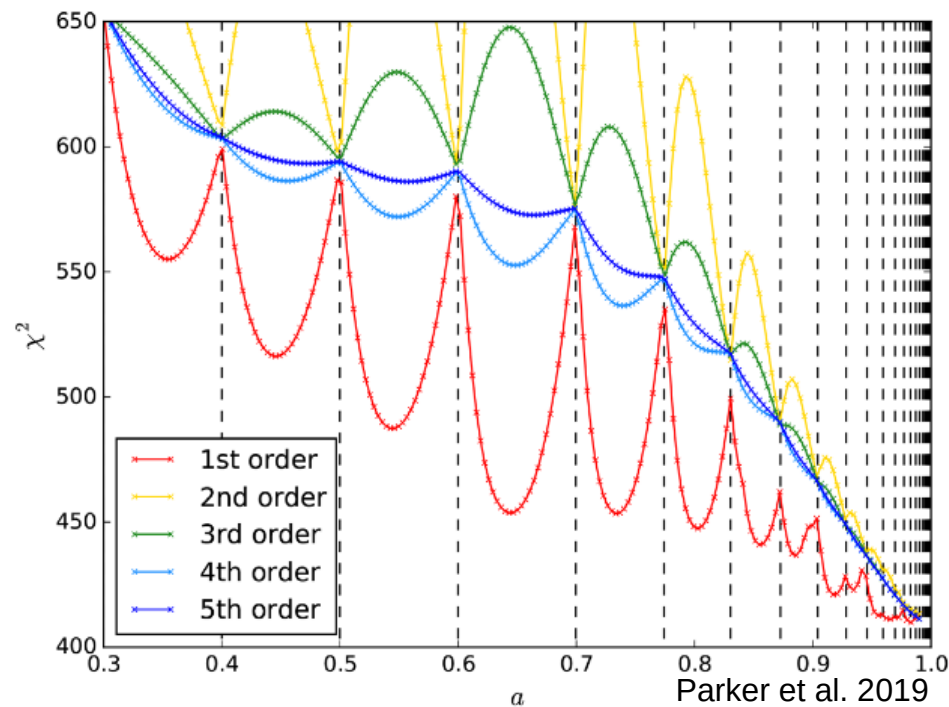
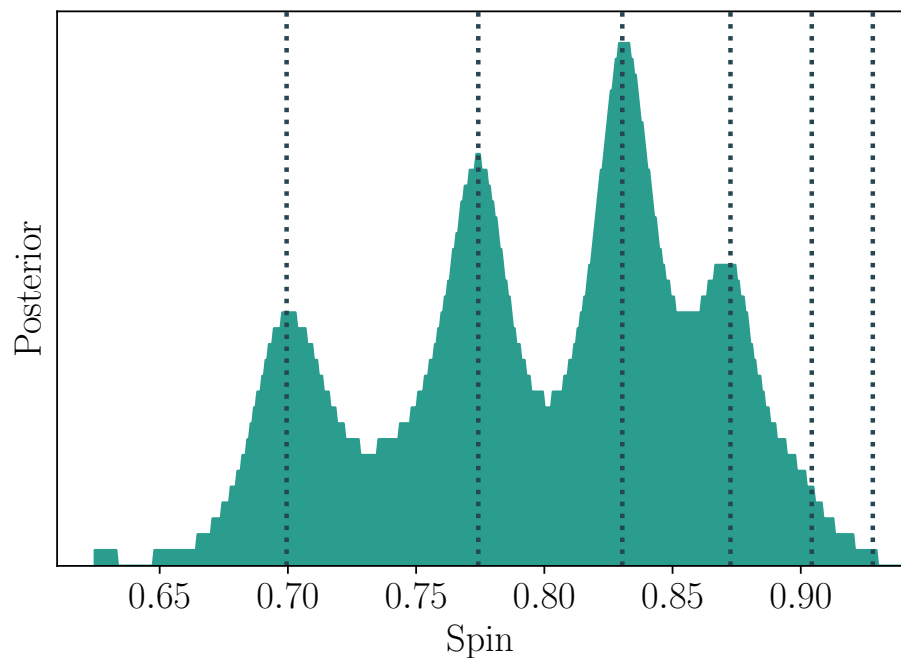


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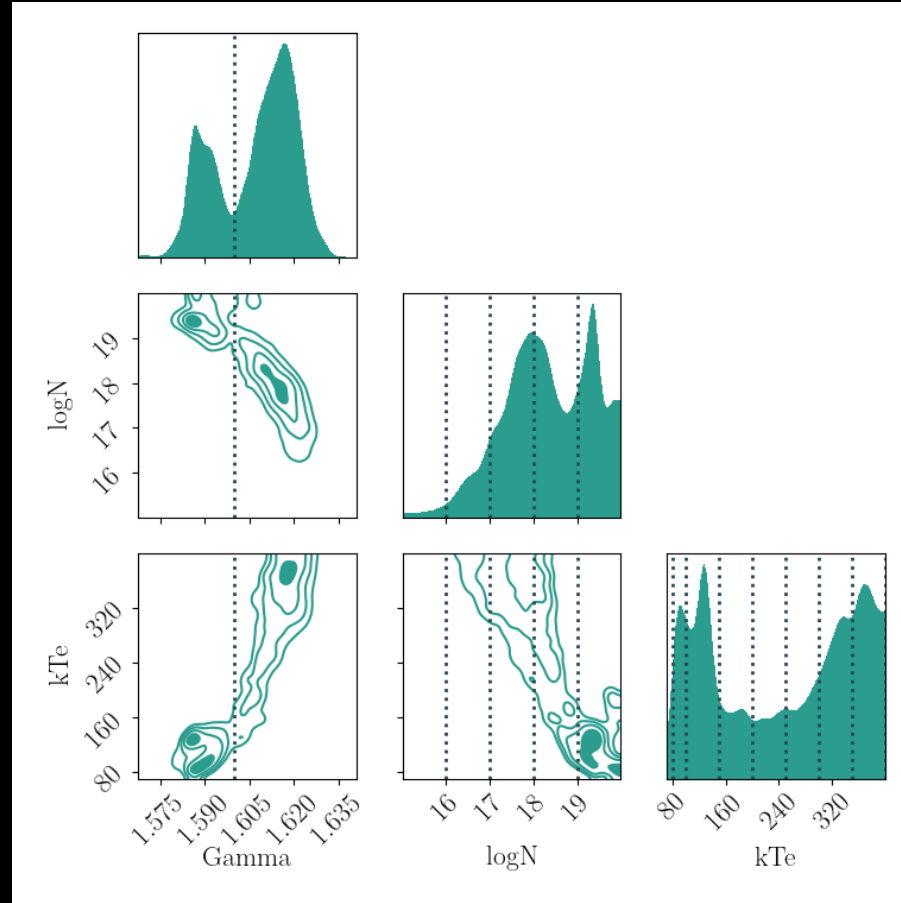
We MUST solve this to measure spin reliably!

# Problematic results: kerrbb

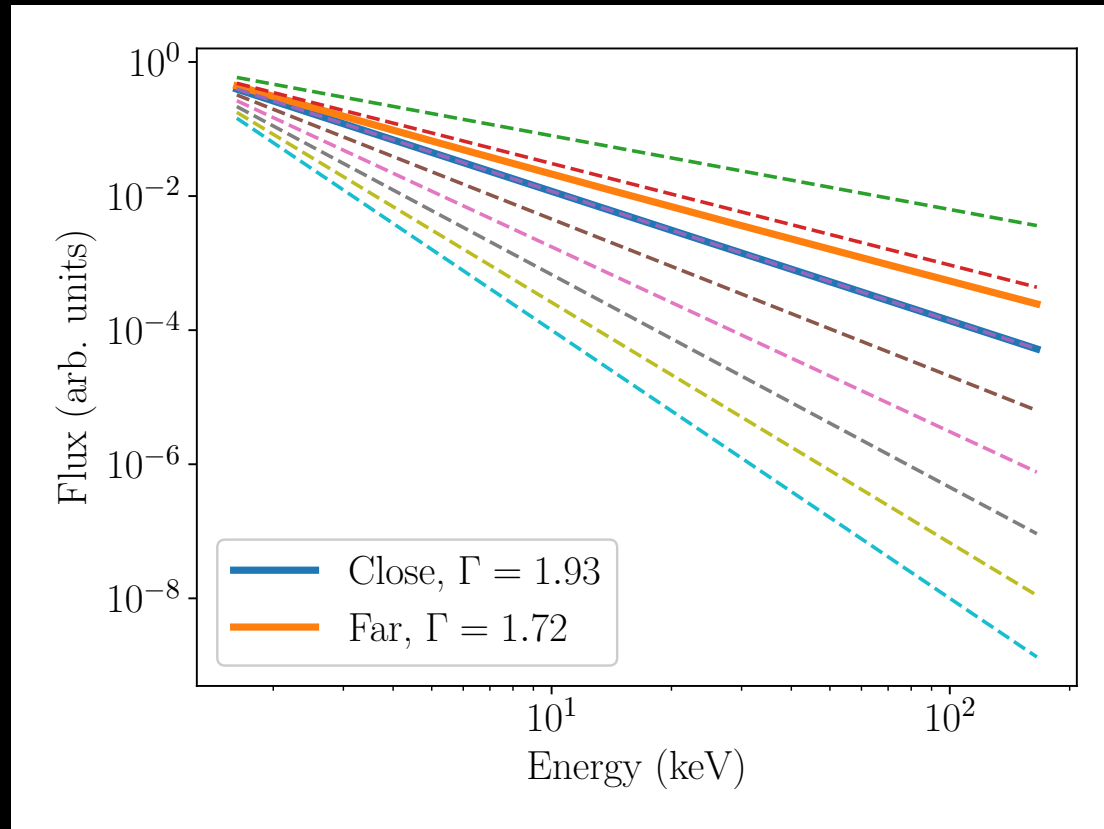


- 1) Samplers and fitters can't find or explore the correct solution
- 2) Model comparison becomes impossible

# It is not just kerrbb!

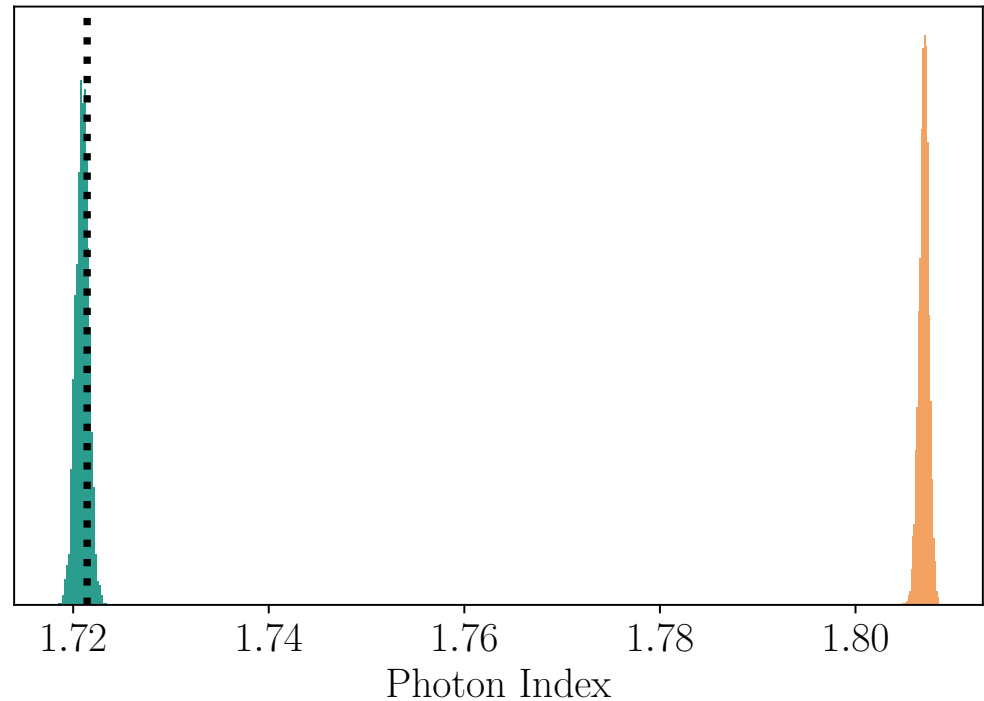
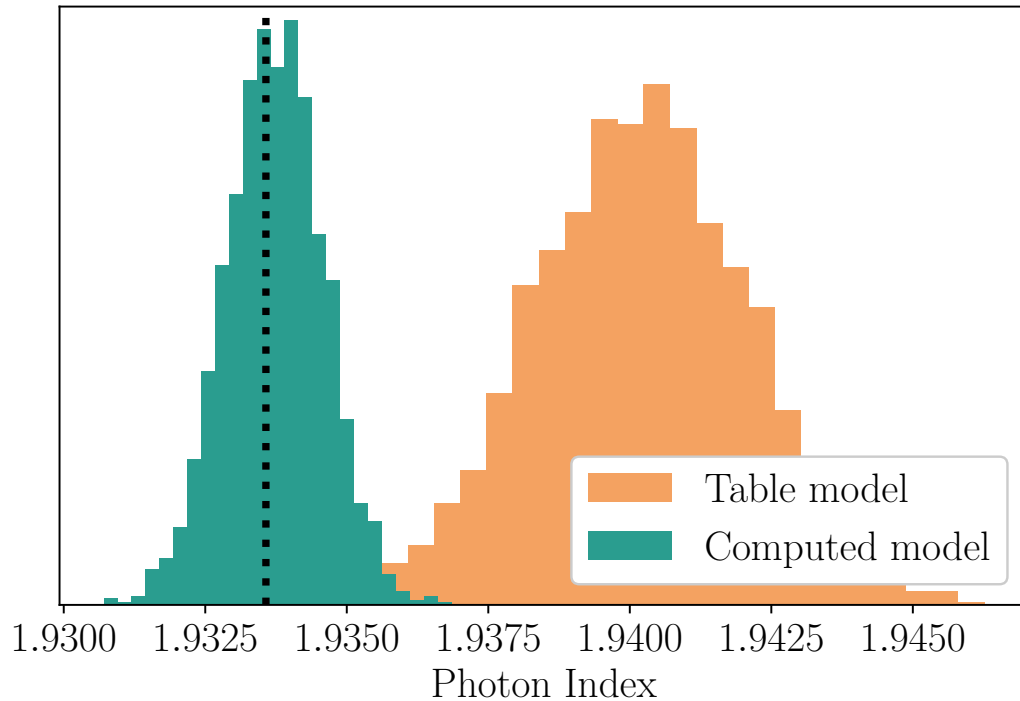


# Additional biases



What happens if I just tabulate a power-law model?

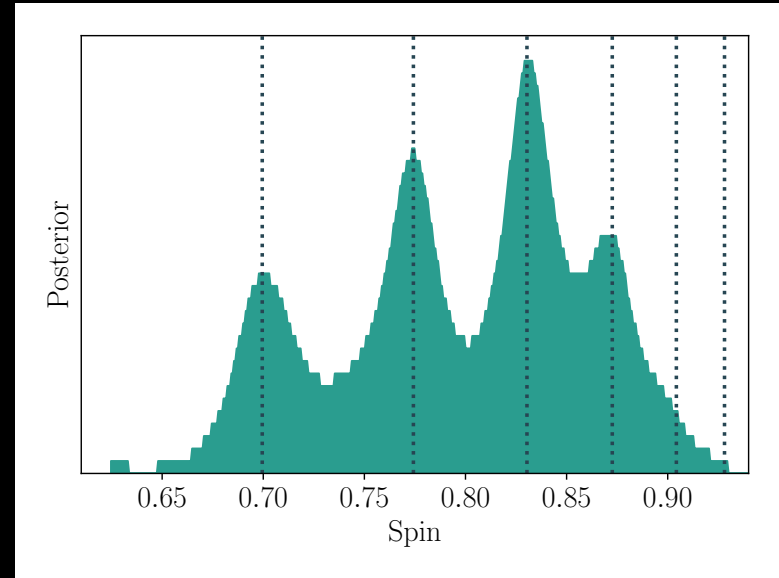
# Additional biases



What happens if I just tabulate a power-law model? Oh no....

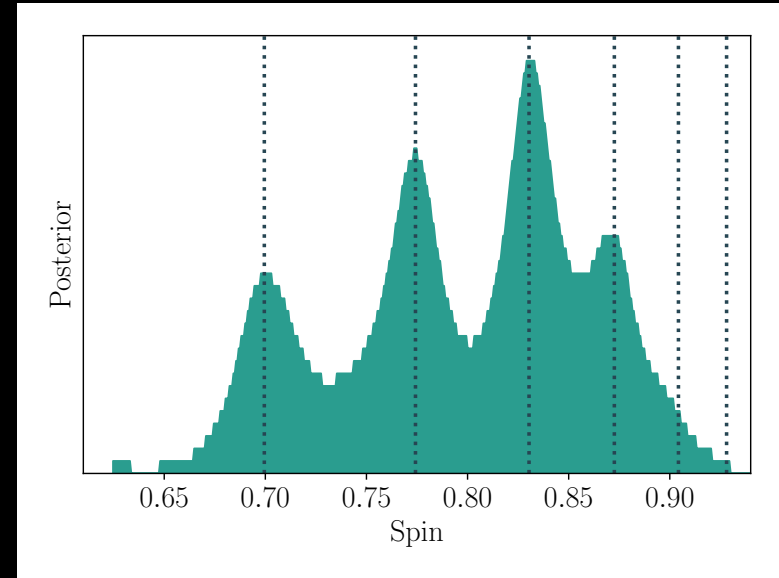
# Conclusions

- X-ray spectroscopy has very fundamental issues with table models! We are making our lives harder than they need to be
- Linear interpolation of table models introduces multi-modality! Modern data demands a new approach



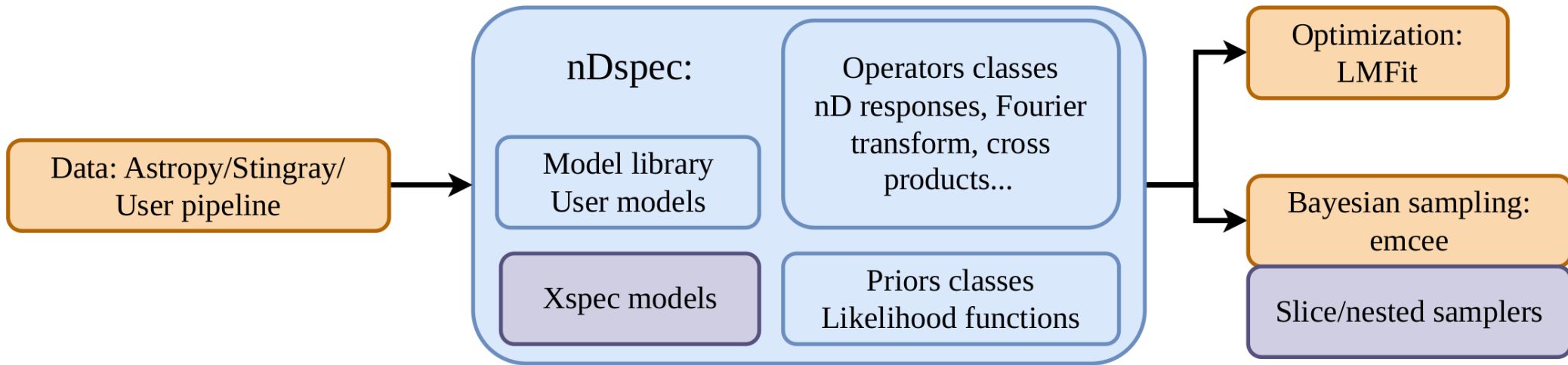
# Conclusions

- X-ray spectroscopy has very fundamental issues with table models! We are making our lives harder than they need to be
- Linear interpolation of table models introduces multi-modality! Modern data demands a new approach
- New instruments require new methods and tools! Exciting to see so much open source software discussed here!
- Where do we go next? See next talk!





# nDspec structure

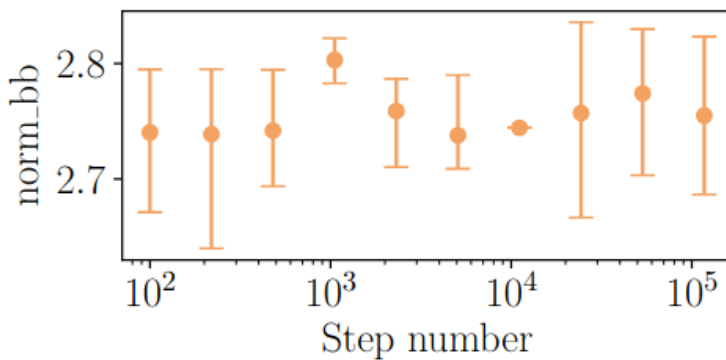
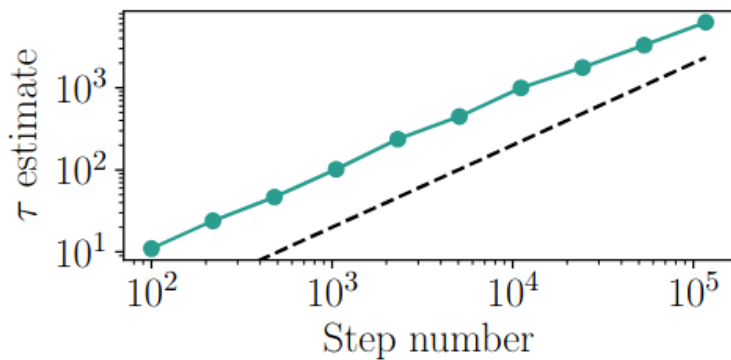
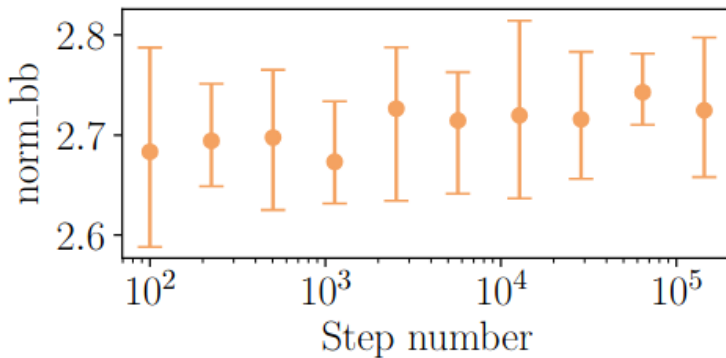
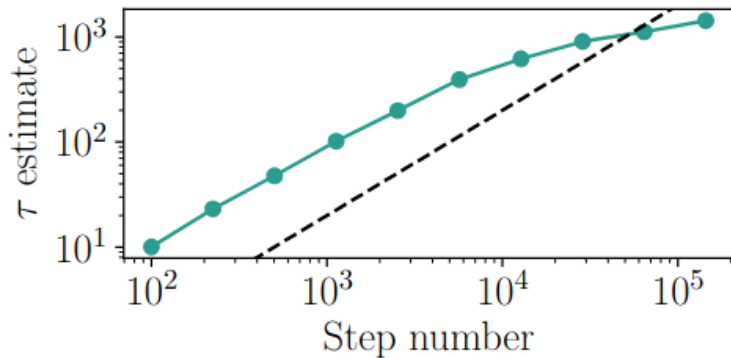


Tie **existing libraries** with **native functionality**

Open architecture allows straightforward **extensions** to additional codes

After 2.5 yrs, nDspec has (minimum) feature parity with existing software

# Convergence examples



# Table models and fit statistics

